



The Pegasus Academy Trust

**Formal written calculation of
whole numbers policy**

1. Introduction

- 1.1 Children develop their understanding of the processes of calculation through practical, oral and mental activities. Children develop this understanding using concrete objects, pictorial representation, mental manipulation and oral discussion. This use of a range of structured activities leads to the fluent manipulation of or 'feel' for numbers.
 - 1.2 They develop ways of recording their thinking and calculation methods, use particular methods that apply to special cases, and learn to interpret and use appropriate signs and symbols involved. Children use models and images, such as empty number lines, to support their mental and informal methods of calculation. Explicit links are made between concrete, pictorial and abstract representations of calculations.
 - 1.3 Children's mental methods are strengthened and refined to become fluent and effective. This is accompanied by a refining of their informal methods. Children are taught the links between mental methods, informal methods and formal written methods. They are also taught where mental methods are different to formal written methods and how to choose the appropriate approach to a given calculation. When faced with a calculation, children are able to decide which method is most appropriate and have strategies to check its accuracy.
 - 1.4 Children are taught formal written methods for addition, subtraction, multiplication and division in appropriate year groups. By the end of Year 6 children are equipped with mental and written methods that they understand and can use correctly.
 - 1.5 Children's learning is underpinned by a secure knowledge of appropriate number facts, the ability to articulate their understanding of key concepts and the methods they have used to solve calculations.
- 1.6 The overall aim is that when children leave the Pegasus Academy Trust they:**
- a) have a secure knowledge of number facts and of the four operations;
 - b) have an efficient, reliable, compact written method of calculation for each operation that children can apply with confidence when undertaking calculations that they cannot carry out mentally.

Year 1 Addition

Year 1 add 1-digit and 2-digit numbers to 20, including zero.

Calculation examples

Adding on a number line

$0 + 0$

Children will add two one digit numbers with a total of up to 20 on a printed number line.

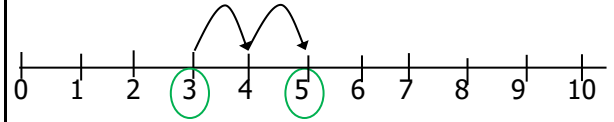
Children circle their start and end points.

MASTERY

Before moving on:

- identify errors e.g. incorrectly circled numbers and incorrect number of jumps
- missing number calculations e.g. $10 + _ = 18$
- explain reasoning verbally

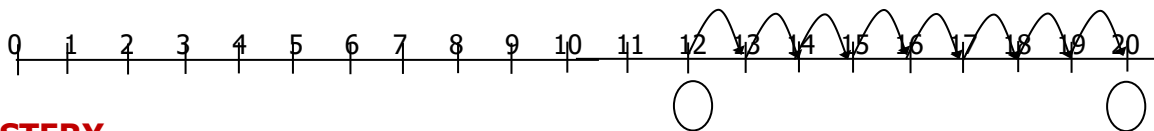
$$3 + 2 = 5$$



$10 + 0$

Children will add a one digit number to a two digit number totalling up to 20 on a printed number line.

$$12 + 8 = 20$$



MASTERY

Before moving on:

- identify errors e.g. incorrectly circled numbers and incorrect number of jumps
- missing number calculations e.g. $10 + _ = 18$
- explain reasoning verbally

Year 1

Subtraction

Year 1 subtract 1-digit and 2-digit numbers to 20, including zero.

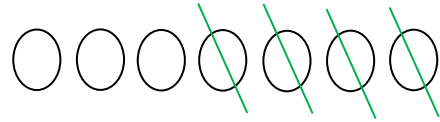
Calculation examples

Pictorial representation

0 - 0

Children will subtract two one digit numbers using an independently drawn pictorial representation. This follows on from children using concrete objects such as counters.

$$7 - 4 = 3$$



Year 1 subtract 1-digit and 2-digit numbers to 20, including zero.

Calculation examples

Subtraction on a number line

0 - 0

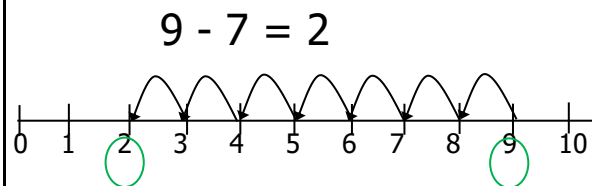
Children will subtract two one digit numbers by counting back on a printed number line.

Children circle their start and end points.

MASTERY

Before moving on:

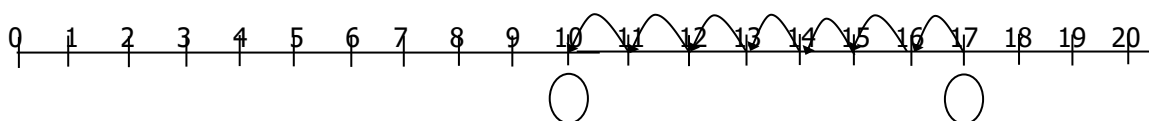
- identify errors e.g. incorrectly circled numbers and incorrect number of jumps
- missing number calculations e.g. $10 - _ = 3$
- explain reasoning verbally



TO - 0

Children will subtract a one digit number from a two digit number less than 20 on a printed number line.

$$17 - 7 = 10$$



MASTERY

Before moving on:

- identify errors e.g. incorrectly circled numbers and incorrect number of jumps
- missing number calculations e.g. $18 - _ = 8$
- explain reasoning verbally

Year 2 Addition

Year 2 adding numbers with up to 2 digits

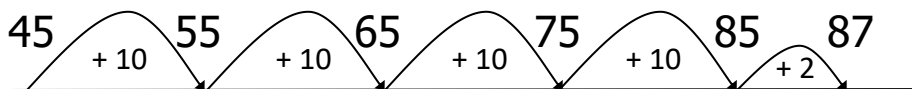
Addition on an empty number line using partitioning

TO + TO *no bridging*

Children will add two 2-digit numbers on an independently drawn empty number line. The number with the least value is partitioned. Children add the 10s first in multiples, then the ones.

$$45 + 42 =$$

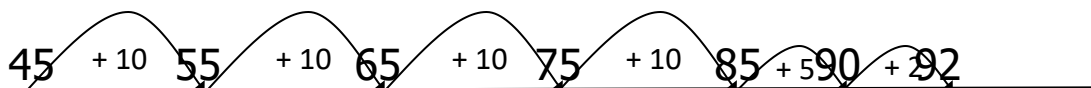
$$\begin{array}{r} 40 \\ 2 \end{array}$$



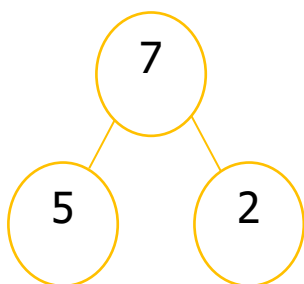
TO + TO *with bridging*

$$45 + 47 =$$

$$\begin{array}{r} 40 \\ 7 \end{array}$$



Children will add two 2-digit numbers on an independently drawn empty number line. The number with the least value is partitioned. Children add the 10s first in multiples, then the ones using their understanding of part-part-whole to bridge the 10.



Year 2 adding numbers with up to 2 digits

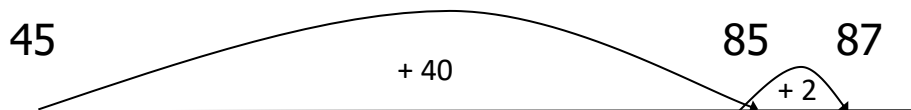
Addition on an empty number line using partitioning

TO + TO *in two steps*

Children will add two 2-digit numbers on an independently drawn empty number line. The number with the least value is partitioned. Children add the 10s in one step, then the ones in the second step.

$$45 + 42 =$$

$$\begin{array}{c} 40 \quad 2 \\ \swarrow \quad \searrow \end{array}$$



MASTERY

Before moving on:

- can children correct calculations with errors
- identify missing digits
- explain reasoning verbally and in writing

Year 2 adding numbers with up to 2 digits	Calculation examples
<p><u>Partitioning and recombining</u></p> <p>TO + TO <i>no bridging</i></p> <p>Children will add numbers with up to 3 digits using brackets to reinforce place value.</p>	$ \begin{array}{r} \text{T O} \\ 43 \\ \swarrow \searrow \\ 40 \quad 3 \end{array} + \begin{array}{r} \text{T O} \\ 34 \\ \swarrow \searrow \\ 30 \quad 4 \end{array} $ $ \begin{aligned} &= (40 + 30) + (3 + 4) \\ &= 70 + 7 \\ &= 77 \end{aligned} $
<p>TO + TO <i>with bridging</i></p> <p>In this calculation stage, the repartitioning of 16 into 10 and 6 will only be necessary for some pupils.</p>	$ \begin{array}{r} \text{T O} \\ 59 \\ \swarrow \searrow \\ 50 \quad 9 \end{array} + \begin{array}{r} \text{T O} \\ 27 \\ \swarrow \searrow \\ 20 \quad 7 \end{array} $ $ \begin{aligned} &= (50 + 20) + (9 + 7) \\ &= 70 + 16 \\ &= (70 + 10) + 6 \\ &= 80 + 6 \\ &= 86 \end{aligned} $

Year 2

Subtraction

Year 2 subtract numbers using concrete objects and pictorial representations, including:
 A 2-digit number and ones,
 A 2-digit number and tens
 Two 2-digit numbers

Calculation examples

Subtraction on a number line

TO - TO *multiples of ten*

Children will subtract a two digit multiple of 10 from a two-digit number by counting back in multiples of 10 on an empty number line that they have drawn.

MASTERY

Before moving on:

- identify errors e.g. incorrectly completed number lines
- missing numbers
- explain reasoning verbally

TO - TO *with partitioning*

Children subtract a two digit number from a two-digit number.

The smaller number is first partitioned into tens and ones. The tens are subtracted first and then the ones.

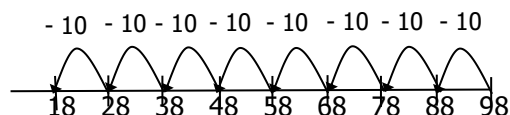
At this stage, calculations do not bridge the tens.

MASTERY

Before moving on:

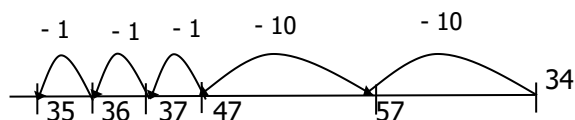
- identify errors e.g. incorrectly completed number lines
- missing numbers
- explain reasoning verbally

$$98 - 80 = 18$$



$$57 - 23 = 34$$

$$\begin{array}{r} 20 \\ 3 \end{array}$$



Year 2 subtract numbers using concrete objects and pictorial representations, including:
 A 2-digit number and ones,
 A 2-digit number and tens
 Two 2-digit numbers

Calculation examples

Subtraction on a number line

TO - TO *with partitioning*

As children become more proficient, they should complete the calculation in fewer steps.

MASTERY

Before moving on:

- identify errors e.g. incorrectly completed number lines
- missing numbers
- explain reasoning verbally

TO - TO *bridging ten*

Children apply mental strategies for bridging ten.

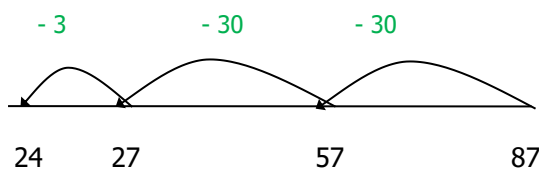
MASTERY

Before moving on:

- identify errors e.g. incorrectly completed number lines
- missing numbers
- explain reasoning verbally

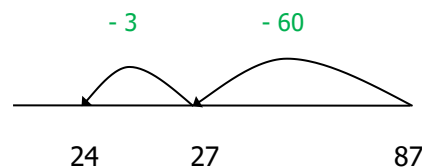
$$87 - 63 = 24$$

$$\begin{array}{r} 60 \\ 3 \end{array}$$



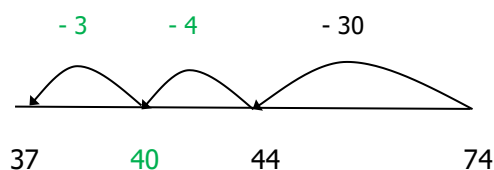
$$87 - 63 = 24$$

$$\begin{array}{r} 60 \\ 3 \end{array}$$



$$74 - 37 = 37$$

$$\begin{array}{r} 30 \\ 3 + 4 \end{array}$$



Year 2

Multiplication

<p>Year 2 solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in context.</p>	<p>Calculation examples</p>
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Multiplication using arrays

0 x 0

Children use arrays to represent the number of multiples, e.g. the four arrays represent the four multiples of two.

This representation can be taught in context: if you have 4 boats with two people in each, how many people are there?

$4 \times 2 = 8$



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Year 3 Addition

Year 3 add numbers with up to three digits, using formal written methods of columnar addition.	Calculation examples
<p><u>Expanded column addition:</u></p> <p>HTO + HTO <i>no bridging</i></p> <p>Children will add numbers with up to 3 digits using columns to reinforce place value.</p> <p>Start by adding the column of least significant value: please model to the children that we always start adding the ones column first.</p>	$ \begin{array}{r} \text{HTO} \quad \text{HTO} \\ 235 \quad + \quad 162 \\ \\ 200 + 30 + 5 \\ + \quad 100 + 60 + 2 \\ \hline 300 + 90 + 7 \\ \hline = 397 \end{array} $
<p><u>Expanded column addition:</u></p> <p>HTO + HTO <i>bridging 10</i></p> <p>The first stage is bridging 10. Children are taught to carry the ten from the ones column into the tens column and recording it above.</p> <p>Planning: please consider carefully the numbers children are adding. At this stage, the children should only be bridging 10.</p>	$ \begin{array}{r} \text{HTO} \quad \text{HTO} \\ 348 \quad + \quad 129 \\ \\ \quad \quad \quad 10 \\ + \quad 300 + 40 + 8 \\ \quad 100 + 20 + 9 \\ \quad 400 + 70 + 7 \\ \hline = 477 \end{array} $

Year 3 add numbers with up to three digits, using formal written methods of columnar addition.	Calculation examples
<p><u>Expanded column addition:</u></p> <p>HTO + HTO <i>bridging 100</i></p> <p>The second stage is bridging 100. Children are taught to carry the hundred from the tens column into the hundreds column, recording it above.</p> <p>Planning: please consider carefully the numbers children are adding. At this stage, the children should only be bridging 100.</p>	$ \begin{array}{r} \text{HTO} \quad \quad \text{HTO} \\ 697 \quad + \quad 281 \\ \\ 100 \\ + 600 + 90 + 7 \\ 200 + 80 + 1 \\ 900 + 70 + 8 \\ \hline = 978 \end{array} $
<p><u>Expanded column addition:</u></p> <p>HTO + HTO <i>bridging 10 and 100</i></p> <p>The final stage is bridging 10 and 100. Children are taught to combine the taught skills in one calculation.</p> <p>Planning: please consider carefully the numbers children are adding. At this stage, the children should be bridging 10 and 100.</p>	$ \begin{array}{r} \text{HTO} \quad \quad \text{HTO} \\ 477 \quad + \quad 264 \\ \\ 100 \quad 10 \\ 400 + 70 + 7 \\ + 200 + 60 + 4 \\ 700 + 40 + 1 \\ \hline = 741 \end{array} $

Year 3

Subtraction

Year 3 subtract numbers with up to three digits, using formal written methods of columnar subtraction	Calculation examples
<p><u>Expanded column subtraction:</u></p> <p>TO - TO <i>no exchange</i></p> <p>Children will subtract numbers with up to 3 digits using columns to reinforce place value.</p> <p>Start by subtracting the column of least significant value: please model to the children that we always start subtracting in the ones column first.</p> <p>Move on to HTO - HTO</p>	$\begin{array}{r} \text{T O} \quad \text{T O} \\ 67 - 42 \\ \\ 60 + 7 \\ - 40 + 2 \\ \hline 20 + 5 \\ \hline = 25 \end{array}$
<p><u>Expanded column subtraction:</u></p> <p>TO - TO <i>with exchange from the 10s column</i></p> <p>The first stage is exchanging from the 10s column into the ones column.</p> <p>Planning:</p> <ul style="list-style-type: none"> • please consider carefully the numbers children are subtracting. At this stage, the children should only be exchanging from the 10s column. • All children will need use Diennes and other concrete resources to understand what exchange is and why it is necessary. <p>MASTERY Before moving on:</p> <ul style="list-style-type: none"> • can children correct calculations with errors • identify missing digits • Explain their reasoning verbally and in writing 	$\begin{array}{r} \text{T O} \quad \text{T O} \\ 82 - 59 \\ \\ 70 \quad 12 \\ - 80 + 2 \\ 50 + 9 \\ - 20 + 3 \\ \hline = 23 \end{array}$

Year 3 subtract numbers with up to three digits, using formal written methods of columnar subtraction

Calculation examples

Expanded column subtraction:

HTO - HTO *with exchange from the 100s column*

The second stage is exchanging from the 100s column into the 10s column.

Planning:

- please consider carefully the numbers children are subtracting. At this stage, the children should only be exchanging from the 100s column.

MASTERY

Before moving on:

- can children correct calculations with errors
- identify missing digits
- Explain their reasoning verbally and in writing

$$\begin{array}{r} \text{HTO} \quad \text{HTO} \\ 316 - 174 \end{array}$$

$$\begin{array}{r} 200 \quad 110 \\ 300 + 10 + 6 \\ - 100 + 70 + 4 \\ \hline 100 + 40 + 2 \\ \hline = 142 \end{array}$$

Expanded column subtraction:

HTO - HTO *with two exchanges*

The third stage is exchanging from the 100s and 10s column in one calculation.

MASTERY

Before moving on:

- can children correct calculations with errors
- identify missing digits
- Explain their reasoning verbally and in writing

$$\begin{array}{r} \text{HTO} \quad \text{HTO} \\ 426 - 238 \end{array}$$

$$\begin{array}{r} 110 \\ 300 \quad 10 \quad 16 \\ 400 + 20 + 6 \\ 200 + 30 + 8 \\ - 100 + 80 + 8 \\ \hline = 188 \end{array}$$

Year 3 subtract numbers with up to three digits, using formal written methods of columnar subtraction	Calculation examples
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Expanded column subtraction:

HTO - HTO *with a 0 in the ones column*

The fourth stage is exchanging from the 10s column when there is a 0 in the ones column.

Planning:

- please consider carefully the numbers children are subtracting. At this stage, there should be only one exchange.

The next stage is HTO - HTO with a 0 in the 10s column, again there should be only one exchange (e.g. 304 - 122).

MASTERY

Before moving on:

- can children correct calculations with errors
- identify missing digits
- Explain their reasoning verbally and in writing

$$\begin{array}{r}
 \text{HTO} \quad \text{HTO} \\
 290 - 176 \\
 \\
 \quad \quad \quad 80 \quad 10 \\
 200 + \cancel{90} + 0 \\
 100 + \cancel{70} + 6 \\
 - \quad \quad \quad 100 + \cancel{10} + \\
 \hline
 \quad \quad \quad 4 \\
 \hline
 = \cancel{114}
 \end{array}$$

Year 3

Multiplication

Year 3 multiplying 2 digits by 1 digit	Calculation examples						
<p><u>Grid method:</u></p> <p>TO x O</p> <p>Children will multiply 2 digit by 1 digit numbers using the grid method to partition beginning with smaller numbers.</p> <p>Planning:</p> <ul style="list-style-type: none"> • All children will need to use Diennes and other concrete resources to support and reinforce their learning. 	<p style="color: #00aaff;">T O</p> <p>1 2 x 4</p> <p>10 \ 2</p> <p>X 10 2</p> <table style="margin-left: auto; margin-right: auto; border-collapse: collapse;"> <tr> <td style="border-right: 1px solid black; border-bottom: 1px solid black; padding: 5px;">4</td> <td style="border-right: 1px solid black; border-bottom: 1px solid black; padding: 5px;">40</td> <td style="border-bottom: 1px solid black; padding: 5px;">8</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"></td> <td style="border-right: 1px solid black; padding: 5px;">40</td> <td style="padding: 5px;">+ 8 = 48</td> </tr> </table>	4	40	8		40	+ 8 = 48
4	40	8					
	40	+ 8 = 48					
<p>When secure, they will move on to larger numbers.</p> <p style="color: #00aaff;">Children would be expected to use the formal column addition method they have already learnt to add the totals from the grid.</p> <p>MASTERY</p> <p>Before moving on:</p> <ul style="list-style-type: none"> • can children correct calculations with errors • identify missing digits • Explain their reasoning verbally and in writing 	<p style="color: #00aaff;">T O</p> <p>8 9 x 7</p> <p>80 \ 9</p> <p>X 80 9</p> <table style="margin-left: auto; margin-right: auto; border-collapse: collapse;"> <tr> <td style="border-right: 1px solid black; border-bottom: 1px solid black; padding: 5px;">7</td> <td style="border-right: 1px solid black; border-bottom: 1px solid black; padding: 5px;">560</td> <td style="border-bottom: 1px solid black; padding: 5px;">63</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"></td> <td style="border-right: 1px solid black; padding: 5px; color: #00aaff;">560</td> <td style="padding: 5px; color: #00aaff;">+ 63 = 623</td> </tr> </table>	7	560	63		560	+ 63 = 623
7	560	63					
	560	+ 63 = 623					

Grid method:

TO x O

Children will multiply 2 digit by 1 digit numbers using the grid method to partition beginning with smaller numbers.

Planning:

- All children will need to use Diennes and other concrete resources to support and reinforce their learning.

T O

1 2 x 4

10 \ 2

X 10 2

4	40	8
	40	+ 8 = 48

When secure, they will move on to larger numbers.

Children would be expected to use the formal column addition method they have already learnt to add the totals from the grid.

MASTERY

Before moving on:

- can children correct calculations with errors
- identify missing digits
- Explain their reasoning verbally and in writing

T O

8 9 x 7

80 \ 9

X 80 9

7	560	63
	560	+ 63 = 623

Year 4 Addition

<p>Year 4 add numbers with up to 4-digits using the formal written methods of columnar addition.</p>	<p>Calculation examples</p>
<p><u>Compact column addition:</u></p> <p>ThHTO + ThHTO <i>no exchange</i></p> <p>The first stage is compact column addition with no carrying.</p> <p>Planning: please consider carefully the numbers children are adding. At this stage, the children should not be carrying.</p> <p>MASTERY Before moving on:</p> <ul style="list-style-type: none"> • can children correct calculations with errors • identify missing digits • Explain their reasoning verbally and in writing 	$ \begin{array}{r} \text{Th H T O} \quad \quad \text{Th H T O} \\ 2\ 3\ 4\ 1 \quad + \quad 1\ 6\ 1\ 3 \\ \\ 2\ 3\ 4\ 1 \\ 1\ 6\ 1\ 3 \\ +\ 3\ 9\ 5\ 4 \\ \hline \hline \end{array} $
<p><u>Compact column addition:</u></p> <p>ThHTO + ThHTO <i>bridging 10</i></p> <p>The second stage is bridging through 10.</p> <p>Please make sure carried digits are in line with the relevant column.</p> <p>Planning: please consider carefully the numbers children are adding. At this stage, the children should be bridging 10 only.</p> <p>MASTERY Before moving on:</p> <ul style="list-style-type: none"> • can children correct calculations with errors • identify missing digits • Explain their reasoning verbally and in writing 	$ \begin{array}{r} \text{Th H T O} \quad \quad \text{Th H T O} \\ 2\ 2\ 5\ 4 \quad + \quad 1\ 6\ 3\ 8 \\ \\ \quad \quad \quad 1 \\ 2\ 2\ 5\ 4 \\ 1\ 6\ 3\ 8 \\ +\ 3\ 8\ 9\ 2 \\ \hline \hline \end{array} $

<p>Year 4 add numbers with up to 4-digits using the formal written methods of columnar addition.</p>	<p>Calculation examples</p>
<p><u>Compact column addition:</u></p> <p>ThHTO + ThHTO <i>bridging 100</i></p> <p>The third stage is bridging through 100.</p> <p>Planning: please consider carefully the numbers children are adding. At this stage, the children should be bridging 100 only.</p> <p>MASTERY Before moving on:</p> <ul style="list-style-type: none"> • can children correct calculations with errors • identify missing digits • Explain their reasoning verbally and in writing 	$ \begin{array}{r} \text{Th H T O} \quad \text{Th H T O} \\ 5 \ 4 \ 5 \ 3 \ + \ 1 \ 2 \ 8 \ 5 \\ \\ \\ \\ + \\ \hline \\ \hline \end{array} $
<p><u>Compact column addition:</u></p> <p>ThHTO + ThHTO <i>multiple bridging</i></p> <p>The fourth stage is bridging through 10 and 100.</p> <p>Planning: please consider carefully the numbers children are adding. At this stage, the children should be bridging 10 and 100 only.</p> <p>MASTERY Before moving on:</p> <ul style="list-style-type: none"> • can children correct calculations with errors • identify missing digits • Explain their reasoning verbally and in writing 	$ \begin{array}{r} \text{Th H T O} \quad \text{Th H T O} \\ 3 \ 2 \ 6 \ 4 \ + \ 2 \ 4 \ 5 \ 9 \\ \\ \\ \\ + \\ \hline \\ \hline \end{array} $

Year 4

Subtraction

<p>Year 4 add numbers with up to 4-digits using the formal written methods of columnar addition.</p>	<p>Calculation examples</p>
<p><u>Compact column addition:</u></p> <p>ThHTO + ThHTO <i>bridging 100</i></p> <p>The third stage is bridging through 100.</p> <p>Planning: please consider carefully the numbers children are adding. At this stage, the children should be bridging 100 only.</p> <p>MASTERY Before moving on:</p> <ul style="list-style-type: none"> • can children correct calculations with errors • identify missing digits • Explain their reasoning verbally and in writing 	$ \begin{array}{r} \text{Th H T O} \quad \text{Th H T O} \\ 5 \ 4 \ 5 \ 3 \quad + \quad 1 \ 2 \ 8 \ 5 \\ \\ \quad \quad \quad 1 \\ \quad \quad 5 \ 4 \ 5 \ 3 \\ \quad \quad 1 \ 2 \ 8 \ 5 \\ + \quad 6 \ 7 \ 3 \ 8 \\ \hline \hline \end{array} $
<p><u>Compact column addition:</u></p> <p>ThHTO + ThHTO <i>multiple bridging</i></p> <p>The fourth stage is bridging through 10 and 100.</p> <p>Planning: please consider carefully the numbers children are adding. At this stage, the children should be bridging 10 and 100 only.</p> <p>MASTERY Before moving on:</p> <ul style="list-style-type: none"> • can children correct calculations with errors • identify missing digits • Explain their reasoning verbally and in writing 	$ \begin{array}{r} \text{Th H T O} \quad \text{Th H T O} \\ 3 \ 2 \ 6 \ 4 \quad + \quad 2 \ 4 \ 5 \ 9 \\ \\ \quad \quad \quad 1 \ 1 \\ \quad \quad 3 \ 2 \ 6 \ 4 \\ \quad \quad 2 \ 4 \ 5 \ 9 \\ + \quad 5 \ 7 \ 2 \ 3 \\ \hline \hline \end{array} $

Year 4 Subtract numbers with up to 4-digits using the formal written methods of columnar subtraction.	Calculation examples
<p><u>Compact column subtraction:</u></p> <p>ThHTO - ThHTO <i>with exchange from the 100s column</i></p> <p>Children will subtract numbers with up to 4 digits</p> <p>The third stage is exchanging from the 100s column into the tens column.</p>	$\begin{array}{r} \text{ThHTO} \quad \text{ThHTO} \\ 6874 - 2582 \\ \\ \begin{array}{r} 71 \\ 6874 \\ \cancel{25}82 \\ - 4292 \\ \hline \end{array} \end{array}$
<p><u>Expanded column subtraction:</u></p> <p>ThHTO - ThHTO <i>with multiple exchanges</i></p> <p>The final stage is exchanging from the 10s and 100s column.</p> <p>Planning:</p> <ul style="list-style-type: none"> please consider carefully the numbers children are subtracting. At this stage, the children should only be exchanging from the 10s and 100s column. <p>MASTERY</p> <p>Before moving on:</p> <ul style="list-style-type: none"> can children correct calculations with errors identify missing digits Explain their reasoning verbally and in writing 	$\begin{array}{r} \text{ThHTO} \quad \text{ThHTO} \\ 9472 - 2288 \\ \\ \begin{array}{r} 1 \\ 361 \\ 9472 \\ \cancel{22}88 \\ - 7184 \\ \hline \end{array} \end{array}$

Year 4

Multiplication

Year 4 multiply 3 digit numbers by a 1-digit number using formal written layout.	Calculation examples
<p><u>Expanded column multiplication:</u></p> <p>HTO x O <i>with brackets</i></p> <p>Children will multiply 3 digit by a 1 digit number using expanded column multiplication starting with the column of least significant value.</p> <p>MASTERY Before moving on:</p> <ul style="list-style-type: none"> • can children correct calculations with errors • identify missing digits • Explain their reasoning verbally and in writing 	$ \begin{array}{r} \text{H T O} \\ 212 \times 4 \\ \\ 212 \\ \times 4 \\ \hline 8 \quad (4 \times 2) \\ 40 \quad (4 \times 10) \\ 800 \quad (4 \times 200) \\ 848 \\ \hline \\ \hline \end{array} $
<p>HTO x O <i>without brackets</i></p> <p>Children will multiply 3 digit by a 1 digit number using expanded column multiplication starting with the column of least significant value.</p> <p>Please make sure carried digits are in line with the relevant column.</p> <p>MASTERY Before moving on:</p> <ul style="list-style-type: none"> • can children correct calculations with errors • identify missing digits • Explain their reasoning verbally and in writing 	$ \begin{array}{r} \text{H T O} \\ 275 \times 7 \\ \\ 275 \\ \times 7 \\ \hline 35 \\ 490 \\ \overset{1}{1}400 \\ 1925 \\ \hline \\ \hline \end{array} $

Year 5 Addition

Year 5 add whole numbers with more than 4 digits, including using formal written

Calculation examples

Compact column addition:

HthTthThHTO + HthTthThHTO *multiple bridging*

Continue using compact column addition to add numbers of more than 4 digits.

Planning: Children in Year 5 need to read and write numbers up to 1,000,000.

MASTERY

Before moving on:

- can children correct calculations with errors
- identify missing digits
- Explain their reasoning verbally and in writing

$$238\,396 + 446\,423$$

$$\begin{array}{r} \\ \\ + \\ \hline \\ \hline \end{array}$$

Year 5

Subtraction

Year 5 subtract whole numbers with more than 4 digits, including using formal written methods.

Calculation examples

Compact column subtraction:

HthTthThHTO - HthTthThHTO *multiple exchange*

Continue using compact column subtraction to subtract numbers of more than 4 digits.

Planning: Children in Year 5 need to read and write numbers up to 1,000,000.

MASTERY

Before moving on:

- can children correct calculations with errors
- identify missing digits
- Explain their reasoning verbally and in writing

$$528\ 245 - 254\ 128$$

$$\begin{array}{r} 4\ 1\ 5\ 3\ 1\ 2\ 8\ 2\ 4\ 5 \\ \cancel{2}\ 5\ 4\ 1\ \cancel{2}\ 8 \\ \hline 2\ 7\ 4\ 1\ 1\ 7 \end{array}$$

Year 5

Multiplication

<p>Year 5 multiply numbers up to 4 digits by a 1-digit or 2-digit number using a formal written method, including long multiplication for 2-digit numbers.</p>	<p>Calculation examples</p>
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Short multiplication:

THTO x O

Children will multiply 4 digit by a 1 digit number using short multiplication starting with the column of least significant value.

Please make sure carried digits are in line with the relevant column.

MASTERY
Before moving on:

- can children correct calculations with errors
- identify missing digits
- Explain their reasoning verbally and in writing

T H T O
4 3 8 7 x 4

1 3 2
4 3 8 7
x 4
1 7 5 4 8

Long multiplication:

TO x TO

Children will multiply 2 digit by 2 digit numbers using long multiplication starting with the column of least significant value.

When multiplying by the tens digit of the multiplier, a zero must be used as place holder.

MASTERY
Before moving on:

- can children correct calculations with errors
- identify missing digits
- Explain their reasoning verbally and in Writing

T O T O
7 5 x 1 9

4
7 5
x 1 9
6 7 5
7 5 0
1 4 2 5

4 40 8

Year 5 multiply numbers up to 4 digits by a 1-digit or 2-digit number using a formal written method, including long multiplication for 2-digit numbers.	Calculation examples
<p><u>Long multiplication:</u></p> <p>THO x TO</p> <p>Children will multiply 3 digit by 2 digit numbers using long multiplication.</p> <p>When multiplying by the tens digit of the multiplier, a zero must be used as place holder.</p> <p>MASTERY Before moving on:</p> <ul style="list-style-type: none"> • can children correct calculations with errors • identify missing digits • Explain their reasoning verbally and in writing 	$\begin{array}{r} \text{HTO} \quad \text{TO} \\ 124 \times 26 \\ \hline \end{array}$ $\begin{array}{r} 124 \\ \times 26 \\ \hline 744 \\ 2480 \\ \hline 3224 \end{array}$
<p><u>Long multiplication:</u></p> <p>ThHTO x TO</p> <p>Children will multiply 4 digit by 2 digit numbers using long multiplication.</p> <p>MASTERY Before moving on:</p> <ul style="list-style-type: none"> • can children correct calculations with errors • identify missing digits • Explain their reasoning verbally and in writing 	$\begin{array}{r} \text{ThHTO} \quad \text{TO} \\ 2428 \times 19 \\ \hline \end{array}$ $\begin{array}{r} 2428 \\ \times 19 \\ \hline 21852 \\ 24280 \\ \hline 46132 \end{array}$ <p style="text-align: center;">4 40 8</p>

Year 5 multiply numbers up to 4 digits by a 1-digit or 2-digit number using a formal written method, including long multiplication for 2-digit numbers.

Calculation examples

Long multiplication:

THO x TO

Children will multiply 3 digit by 2 digit numbers using long multiplication.

When multiplying large numbers where there are many carried digits, children would be encouraged to cross through the carried digit already used for 'house-keeping'.

MASTERY

Before moving on:

- can children correct calculations with errors
- identify missing digits
- Explain their reasoning verbally and in writing

Th H T O T O

2 4 2 8 x 3 9

1 2
~~3~~ ~~4~~ ~~7~~ 2 4 2 8
x 3 9

2 1 8 5 2

7 2 8 4 0

9 4 6 9 2

4 40 8

Year 5 Division

Year 5 divide numbers up to 4 digits by a 1-digit number using the formal written method of short division and interpret remainders appropriately for the context.

Calculation examples

Short division:

ThHTO \div O *no remainders*

The expectation is that children will be able to divide a 4 digit by a 1 digit number using short division. Start by dividing into the most significant digit.

This is the first formal written method of division that children will learn. Previously, they will have represented dividing as sharing, grouping and as the inverse of multiplication.

Children must be secure with their understanding of place value:

- The first step is 'how many 3s go into 6000?'
- The 2 in the answer represents 2000 3s.
- There are then 100 3s in 300, 30 3s in 90 and 2 3s in 6.
- The answer shows there are 2132 3s in 6396 or $6396 \div 3 = 2132$.

Planning: the expectation is that children will be able to recall their multiplication and division facts to 12x12 by the end of Y4.

Begin by using digits that are all divisible by the divisor. In the example, each digit is in the 3 times-table.

MASTERY

Before moving on:

- can children correct calculations with errors
- identify missing digits
- explain their reasoning verbally and in writing

$$6396 \div 3 =$$

$$\begin{array}{r} 2132 \\ 3 \overline{) 6396} \end{array}$$

Year 5 divide numbers up to 4 digits by a 1-digit number using the formal written method of short division and interpret remainders appropriately for the context.

Calculation examples

Short division:

ThHTO ÷ O with **one** internal remainder of **1**

The second stage is to include one digit that will leave an internal remainder of 1.

Planning: please consider carefully the numbers children are dividing. At this stage there must only be one internal remainder.

MASTERY

Before moving on:

- children must have the opportunity to record the one remainder in different columns
- can children correct calculations with errors and identify missing digits
- explain their reasoning verbally and in Writing
- Question about place value; what is the value of each digit and what does that mean.
-

$$4236 \div 3 =$$

$$\begin{array}{r} 1412 \\ 3 \overline{) 4236} \\ \underline{3} \\ 12 \\ \underline{12} \\ 0 \\ \underline{0} \\ 0 \end{array}$$

$$4236 \div 3 =$$

$$\begin{array}{r} 2142 \\ 3 \overline{) 6426} \\ \underline{6} \\ 0 \\ \underline{0} \\ 0 \\ \underline{0} \\ 0 \end{array}$$

ThHTO ÷ O with **one** internal remainder greater than 1

The third stage is to include one digit that will leave an internal remainder greater than 1.

Planning: please consider carefully the numbers children are dividing. At this stage there must only be one internal remainder that is greater than 1.

MASTERY

Before moving on:

- See above

$$5136 \div 3 =$$

$$\begin{array}{r} 1712 \\ 3 \overline{) 5136} \\ \underline{3} \\ 21 \\ \underline{21} \\ 0 \\ \underline{0} \\ 0 \\ \underline{0} \\ 0 \end{array}$$

<p>Year 5 divide numbers up to 4 digits by a 1-digit number using the formal written method of short division and interpret remainders appropriately for the context.</p>	<p>Calculation examples</p>
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Short division:

ThHTO \div O *with a digit less than the divisor*

The fourth stage is to divide numbers when a digit is less than the divisor.

Zero must be used as a place holder

Planning: please consider carefully the numbers children are dividing. At this stage there must only be one internal remainder.

MASTERY
Before moving on:

- children must have the opportunity to record the remainder in different columns
- can children correct calculations with errors
- identify missing digits
- explain their reasoning verbally and in writing

$2469 \div 3 =$

$$\begin{array}{r} 0823 \\ 3 \overline{) 2469} \\ \underline{24} \\ 6 \\ \underline{6} \\ 9 \\ \underline{9} \\ 0 \end{array}$$

$3627 \div 3 =$

$$\begin{array}{r} 1209 \\ 3 \overline{) 3627} \\ \underline{36} \\ 2 \\ \underline{21} \\ 7 \\ \underline{6} \\ 1 \end{array}$$

ThHTO \div O

The fifth stage is to include digits that will leave more than one internal remainder and digits less than the divisor.

MASTERY
Before moving on:

- can children correct calculations with errors
- identify missing digits
- explain their reasoning verbally and in writing

$2253 \div 3 =$

$$\begin{array}{r} 0751 \\ 3 \overline{) 2253} \\ \underline{22} \\ 5 \\ \underline{3} \\ 2 \\ \underline{21} \\ 3 \\ \underline{3} \\ 0 \end{array}$$

Year 5 divide numbers up to 4 digits by a 1-digit number using the formal written method of short division and interpret remainders appropriately for the context.

Calculation examples

Short division:

ThHTO \div O *with remainders*

The final stage is to divide numbers that leave a remainder.

Planning: please consider carefully the numbers children are dividing. At this stage there must be remainders.

MASTERY

Before moving on:

- can children correct calculations with errors
- identify missing digits
- explain their reasoning verbally and in writing

$$2437 \div 3 =$$

$$\begin{array}{r} 0812 \text{ r}1 \\ 3 \overline{) 2437} \\ \underline{24} \\ 03 \\ \underline{03} \\ 07 \\ \underline{06} \\ 1 \end{array}$$

Year 6 Division

Year 6 divide numbers up to 4 digits by a 2 digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context.

Calculation examples

Short division:

ThHTO \div TO *no remainders*

The expectation is that children will be able to divide a 4 digit by a 2 digit number using short division. Start by dividing into the most significant digit.

Children must be secure with the division methods taught in Y5.

Children will need to record multiples of the divisor alongside the calculation before attempting to solve it.

MASTERY

Before moving on:

- can children correct calculations with errors
- identify missing digits
- explain their reasoning verbally and in writing

ThHTO \div TO *with remainders*

MASTERY

Before moving on:

- can children correct calculations with errors
- identify missing digits
- explain their reasoning verbally and in writing

$$2750 \div 22 =$$

	0 1 2 5	22
	2 7 5 0	44
22	2 7 5 0	66
	2 7 5 0	88
	2 7 5 0	110

$$3799 \div 18 =$$

	0 2 1 1 r1	18
	3 7 9 9	36
18	3 7 9 9	54
	3 7 9 9	72
	3 7 9 9	90

Year 6 divide numbers up to 4 digits by a 2 digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context.

Calculation examples

Long division:

ThHTO ÷ TO *no remainders*

Children will use long division when short division is no longer the most efficient method.

In the example, the next step is to find the difference between 155 and 132.

If a written subtraction is needed to calculate an internal remainder, long division should be used.

MASTERY

Before moving on:

- can children correct calculations with errors
- identify missing digits
- explain their reasoning verbally and in writing

$$8151 \div 33 =$$

	0 2		33
33	8 1 5 1		66
	8 1 5		99
			132

	0 2 4 7		
33	8 8 1 5 1		33
	6 6		66
	1 5 5		99
	1 3 2		132
	0 2 3 1		165
	2 3 1		198
	0		231

Year 6 divide numbers up to 4 digits by a 2 digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context.

Calculation examples

Long division:

ThHTO \div TO *with remainders*

MASTERY

Before moving on:

- can children correct calculations with errors
- identify missing digits
- explain their reasoning verbally and in writing

	0 1 5 8 r 11	
46	$\begin{array}{r} \overline{) 7279} \\ 46 \\ \underline{267} \\ 230 \\ \underline{0379} \\ 368 \\ \underline{011} \end{array}$	46 92 138 184 230 276 322 368

Year 6 divide numbers up to 4 digits by a 2 digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context.

Calculation examples

$$3438 \div 24$$

Long division:

ThHTO \div TO *with the remainder recorded as a Fraction*

The remainder 6 can be recorded as $\frac{6}{24}$. You will notice that the divisor is the denominator and the remainder is the numerator. This can be simplified to $\frac{1}{4}$.

MASTERY

Before moving on:

- can the children reduce a fraction to its simplest term
- explain their reasoning verbally and in Writing

ThHTO \div TO *with remainders recorded as decimals*

MASTERY

Before moving on:

- can children correct calculations with errors
- identify missing digits
- explain their reasoning verbally and in writing

Remainders can also be calculated as decimals. The remaining ones can be converted to tenths by putting in the place holder and a decimal point in the answer. The remainder of 60 tenths can now be divided by 24. Similarly, the remainder 12 can be converted into 120 hundredths, again by putting in the place holder, and can then be divided by 24.

$$\begin{array}{r}
 0143 \frac{6}{24} \\
 24 \overline{) 3438} \\
 \underline{24} \\
 103 \\
 \underline{96} \\
 78 \\
 \underline{72} \\
 6
 \end{array}$$

$$= 143$$

$$\frac{1}{4}$$

$$3438 \div 24$$

$$\begin{array}{r}
 0143.25 \\
 24 \overline{) 3438} \\
 \underline{24} \\
 103 \\
 \underline{96} \\
 78 \\
 \underline{72} \\
 60 \\
 \underline{48} \\
 120 \\
 \underline{120} \\
 0
 \end{array}$$